

REGISTRATION NUMBER

SRINIX COLLEGE OF ENGINEERING

2nd INTERNAL EXAMINATION 2021-22

Sub- Math-I

1st Semester

Branch-All(A+B)

Full marks-100

Time -2.30hrs

1. Answer all questions (Part – A)

 $(2 \times 10 = 20)$

- a) What is circle of curvature ?
- b) Define stationary point for the function of two variables.
- c) Find the radius of the curvature of the curve $y=e^x$ at the point where it crosses the y-axis.
- d) Write a relationship between Beta and Gamma functions.
- e) Write the standard form of linear differential equation of first order and first degree and give one example.
- f) What is the necessary condition for the extreme value of f(x,y)?
- g) Evaluate $\Gamma(3/2)$.
- h) Find the blank; $\Gamma(n)\Gamma(n-1)=$
- i) Find the asymptotes parallel to x-axis of the curve xy(x-2)-(x+3)(x-1)=0
- j) Find the radius of curvature of the curve r=asino
- 2. Answer any eight questions (Part B) (6x 8 = 48)

a) Solve
$$\frac{dy}{dx} + y = e^{-x}$$

- b) Solve $x(1+y^2)dx-y(1+x^2)dy=0$
- c) Prove that $\Gamma(1/2) = \sqrt{\pi}$
- d) Find the equation of the circle of the curvature associated with the curve $y=x^2(x-1)$.
- e) Show that the curve $re^{\theta} = a(1+\theta)$ has no point of the inflexion.
- f) Find the asymptotes of the hyperbolic spiral $r\theta = a$.
- g) Evaluate $\int_0^\infty e^{-x^2} dx$ by Gamma function.

- h) Apply Newtonian formula to find the radius of curvature at the origin of the cycloid $x=a(\theta + \sin \theta), y=a(1-\cos \theta)$.
- i) Find the asymptotes of the curve $x^2y+xy^2+y^2+3x=0$
- 3. Answer any Two questions (Part C) (16x 2 =32)

a) Solve
$$\frac{dy}{dx}(x^2y^3 + xy) = 1$$

- b) Examine the function $x^2 xy + y^4$ for its extreme values.
- c) Find all the possible asymptotes of the curve $y(x y)^3 = y(x y) + 2$